

# **TI-89/TI-92 Plus/Voyage™ 200 Polynomial Root Finder**

## How To...

- Start the Application
- Enter a Problem
- Solve a Problem

- Graph a Problem
- Store Values
- Navigate

## **Examples**

- Roots of a Third-Degree Polynomial
- Complex Roots
- Complex Coefficients

## **More Information**

- Customer Support
- Notes and Hints

Error Messages



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# What is the Polynomial Root Finder Application?

The Polynomial Root Finder application (App) calculates numeric roots (zeros) of polynomials using the calculator's eigenvalue routines.

The Polynomial Root Finder App provides a convenient, easy-to-use interface to simplify setting up the problem, solving it, and exploring the solution.

You can:

- Edit the coefficients of the polynomial.7
- Load a list for the coefficients.
- Store the solution in a list.
- Graph the polynomial.
- Solve up to 30th-order real or complex polynomials.

# **Entering a Problem**

## **Entering data manually**

1. <u>Start</u> the Polynomial Root Finder App and select **New**.



- 2. Enter the degree of the polynomial. The degree must be an integer between 1 and 30.
- 3. Press ENTER to display the Coefficients screen.
- Enter the first coefficient value. You can enter a real or complex value or an expression that resolves to a real or complex value.
- 5. Press ENTER or  $\odot$  to go to the next coefficient.
- 6. Continue entering coefficient values.
- 7. Press ENTER after entering the last coefficient value.

#### Loading existing data

You can load an existing list as all or part of the problem from within the Polynomial Root Finder App by using either of the following methods.

- Press F2 and select a folder and list.
- Press F1 1:Load Coefficients and select a folder and list.

#### **Editing coefficients**

- 1. If you are on the Solutions screen, press F4 to display the Coefficients screen.
- 2. Move the cursor to a coefficient and change its value.
- 3. Press ENTER to accept the changes.

#### **Clearing coefficients**

Press F1 8:Clear All.

#### **Starting a new problem**

Press F1 3:New Problem.

# **Solving Numerically**

Solutions are always computed numerically, regardless of whether the Exact/Approx mode setting is **Auto**, **Exact**, or **Approximate**. The Polynomial Root Finder App calculates roots numerically by finding the eigenvalues of a corresponding companion matrix.

- 1. Complete the coefficient entry in the Coefficients screen. You must press ENTER to accept the last entered or changed value.
- 2. Press F5 to solve the problem. The numeric values of the roots appear in the Solutions screen. The busy indicator on the status line displays while calculating the solution.
  - Note The roots  $x_1 \dots x_n$  are displayed according to the **Complex** Format mode setting. If the mode is **Real**, complex roots are displayed as **Non-Real** *unless* a complex coefficient was entered.

# **Solving Graphically**

- After entering coefficients, press 2nd [F6] (TI-89) or F6 1:Open Graph. This option is available from either the Coefficients or Solutions screen.
- 2. Select the graphing options and press ENTER.
  - Split Screen Choose 1:Full or 2:Left-Right. (The Top-Bottom option is not available.)
  - Store Poly to Choose a y-variable or choose 1:none to graph without storing.
  - Zoom Choose 1:ZoomRoots, 2:ZoomStd, 3:ZoomFit, or 4:none. ZoomRoots sets the viewing window based on the solutions found by the Polynomial Root Finder App, relative minimums and maximums, and inflection points.

When the graph displays, the standard graph tools such as Zoom, Trace, and Math are available on the tool bar.

## **Displaying graph with coefficients or solutions**

In split screen mode, a thick border indicates the active portion. Press 2nd [I] to switch between the graph and the Coefficients or Solutions portion.

F1+ F2+ F3 F4 ToolsZoomTraceRe9r	F5+ F6+ F7+≶8 aphMathDrawPen⊳
a <sub>3</sub> × <sup>3</sup> ++a <sub>1</sub> ×+a <sub>0</sub> =	
a3=2. a2=-5.	
a <sub>1</sub> =1. a <sub>0</sub> =3.	
MAIN RAD EXAC	



Graph portion is active

Coefficients portion is active

To display the Solutions screen with the graph, switch to the Coefficients portion of the split screen, and press [F5].



Solutions with graph

To return to the Coefficients screen, press F4 from the Solutions screen.

While in split screen mode, you can change the coefficients and recalculate the solutions. The graph does not automatically update for the new values. To update the graph, select [2nd] [F6] (TI-89) or [F6] **1:Open Graph** from the Coefficients or Solutions screen.

## **Quitting the graph**

- 1. Press 2nd [+] to switch to the Coefficients or Solutions screen.
- 2. Press 2nd [F6] (TI-89) or F6 2:Quit Graph.

# Storing

Once you have entered the coefficients, you can store:

- All the coefficients to a list.
- An individual coefficient to a variable.
- The polynomial to a Y= equation.

Once you have calculated the roots, you can store:

- All the roots to a list.
- An individual root to a variable.

To store from either the Coefficients or Solutions screen:

- Press F3 and select one of the following:
  - 1:Coefficients and select a folder and list name.
  - **2:Solutions** and select a folder and list name.
  - **3:Poly to Y= Editor** and select a y-variable.

To store individual coefficients or roots from the Coefficients or Solutions screen:

1. On the Coefficients screen, place the cursor on the value you want to store.

On the Solutions screen, place the cursor on the equal sign (=) of the  $x_i$  value you want to store.

- 2. Press STO►.
- 3. Enter a variable name and press ENTER.

# Navigating Within the Polynomial Root Finder App

- (†) (•) or (†) (•) highlights values on the Coefficients screen. Values can be cut, copied, and pasted.
- 2nd () or 2nd () moves the cursor to the beginning or end of a value on the Coefficients screen.
- 2nd ⊙ or 2nd ⊙ moves the cursor up or down one page on the Coefficients or Solutions screen.
- [Ind] [Ind] toggles between applications or between split screen portions.

## **Notes and Hints**

- Radian angle mode is recommended for complex number calculations if the Complex Format mode setting is Polar. Internally, the TI-89 / TI-92 Plus / Voyage<sup>™</sup> 200 PLT converts all entered trigonometry values to radians, but it does not convert values for exponential, logarithmic, or hyperbolic functions.
- The values of non-real roots are shown on the Solutions screen only if the Complex Format mode setting is Rectangular or Polar. If the format is Real, the Solutions screen displays Non-Real.
- 0 is not a valid entry for a<sub>n</sub>. If you press ENTER on any other coefficient without entering a value, 0 is entered automatically. If you press ENTER on a<sub>n</sub> without entering a value, 1 is entered automatically.

## **Example — Roots of a Third-Degree Polynomial**

Find the roots of  $2x^3 - 5x^2 + x + 3 = 0$ .

- 1. <u>Start</u> the Polynomial Root Finder App and select **New**.
- 2. Press **3** ENTER for a third-degree polynomial.
- 3. Enter the coefficients:  $a_3 = 2$ ,  $a_2 = -5$ ,  $a_1 = 1$ ,  $a_0 = 3$ .
- 4. Press F5 to solve the problem. The busy indicator on the status line displays while the solution is calculated.

The values for  $x_1$ ,  $x_2$ , and  $x_3$  are displayed:

 $x_1 = -.618034$  $x_2 = 1.5$  $x_3 = 1.61803$ 

## **Example — Complex Roots**

Find the roots of  $x^3 + x^2 + x + 1 = 0$ .

- 1. Press MODE and set Angle to Radian and Complex Format to Real.
- 2. <u>Start</u> the Polynomial Root Finder App and select **New**.
- 3. Press **3** ENTER for a third-degree polynomial.
- 4. Enter the coefficients:  $a_3 = 1$ ,  $a_2 = 1$ ,  $a_1 = 1$ ,  $a_0 = 1$ .
- 5. Press F5 to solve the problem. The busy indicator on the status line displays while the solution is calculated.

The values for  $x_1$ ,  $x_2$ , and  $x_3$  are displayed:

 $x_1 = -1.$  $x_2 = Non-Real$  $x_3 = Non-Real$ 

## **Example — Complex Coefficients**

Find the roots of 15  $x^3 - 4i x^2 + (7+i) x + 2i = 0$ .

- 1. Press MODE and set Angle to Radian and Complex Format to Rectangular.
- 2. <u>Start</u> the Polynomial Root Finder App and select New.
- 3. Press **3** ENTER for a third-degree polynomial.
- 4. Enter the coefficients:  $a_3 = 15$ ,  $a_2 = -4i$ ,  $a_1 = 7+i$ ,  $a_0 = 2i$ .
- 5. Press F5 to solve the problem. The busy indicator on the status line displays while the solution is calculated.

The values for  $x_1$ ,  $x_2$ , and  $x_3$  are displayed:

x<sub>1</sub> = <sup>-</sup>.038274+.926765\**i* x<sub>2</sub> = <sup>-</sup>.174161-.282031\**i* x<sub>3</sub> = .212435-.378067\**i* 

# **Errors, Error Messages, and Restrictions**

Message	What To Do
Highest degree polynomial coefficient cannot be zero.	You must enter a nonzero value for a <sub>n</sub> .
All functions are in use. Clear unnecessary functions from the Y= Editor.	Press • [Y=] and clear any unnecessary functions.
Memory	The Polynomial Root Finder App requires at least 3000 bytes of RAM to run properly. When the amount of available RAM falls below this threshold, the application may display an <b>Error: Memory</b> dialog box and return to the Home screen or simply exit to the Home screen. If this occurs, archive or delete some variables before returning to the application.

# Installing the Polynomial Root Finder App

Detailed Flash application installation instructions are available from <u>education.ti.com/guides</u>.

You will need:

- A TI-89 / TI-92 Plus / Voyage<sup>™</sup> 200 PLT with the latest Advanced Mathematics Software Operating System. Download a free copy from <u>education.ti.com/softwareupdates</u>.
- A computer using either Microsoft<sup>®</sup> Windows<sup>®</sup> or Apple<sup>®</sup> Macintosh<sup>®</sup> operating system software.
- A TI-GRAPH LINK<sup>™</sup> computer-to-calculator cable, available for purchase from the <u>TI Online Store</u>.
- Either TI Connect<sup>™</sup> software or TI-GRAPH LINK connectivity software for the TI-89 / TI-92 Plus. Download a free copy from <u>education.ti.com/softwareupdates</u>.

# **Starting and Quitting the Application**

#### **Starting the Polynomial Root Finder App**

The instructions in this guidebook refer to this Flash application only. For help using this product, refer to the comprehensive guidebook at <u>education.ti.com/guides</u>.

- 1. Press [APPS] and select Polynomial Root Finder.
- 2. Select the problem type from the menu.
  - Current returns to the screen you were on when you left the Polynomial Root Finder App.
  - Open lets you select an <u>existing list</u> to use as the coefficients of the polynomial.
  - New creates a <u>new problem</u>.

## **Quitting the Polynomial Root Finder App**

Press 2nd [QUIT] from any screen.

# **Deleting an Application**

Deleting an application removes it from the handheld device and increases space for other applications. Before deleting an application, consider storing it on a computer for reinstallation later.

- 1. Quit the application.
- 2. Press [2nd] [VAR-LINK] to display the VAR-LINK [ALL] screen.
- 3. Press 2nd [F7] (TI-89) or F7 to display the list of installed applications.
- 4. Select the application you want to delete.
- 5. Press F1 1:Delete. The VAR-LINK delete confirmation dialog box displays.
- 6. Press ENTER to delete the application.

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## Page Reference

This PDF document contains electronic bookmarks for on-screen navigation. If you print this document, use the page numbers below to find specific topics.

Important Information	2
What is the Polynomial Root Finder Application?	3
Entering a Problem	4
Solving Numerically	6
Solving Graphically	7
Storing	10
Navigating Within the Polynomial Root Finder App	12
Notes and Hints	13
Example — Roots of a Third-Degree Polynomial	14
Example — Complex Roots	15
Example — Complex Coefficients	16
Errors, Error Messages, and Restrictions	17
Installing the Polynomial Root Finder App	18
Starting and Quitting the Application	19
Deleting an Application	20
Texas Instruments (TI) Support and Service Information	21
TEXAS INSTRUMENTS LICENSE AGREEMENT	22