



Div. Ingeniería de Sistemas y Automática

Universidad Miguel Hernández

Current Subjects in Computer Science

Segmentation



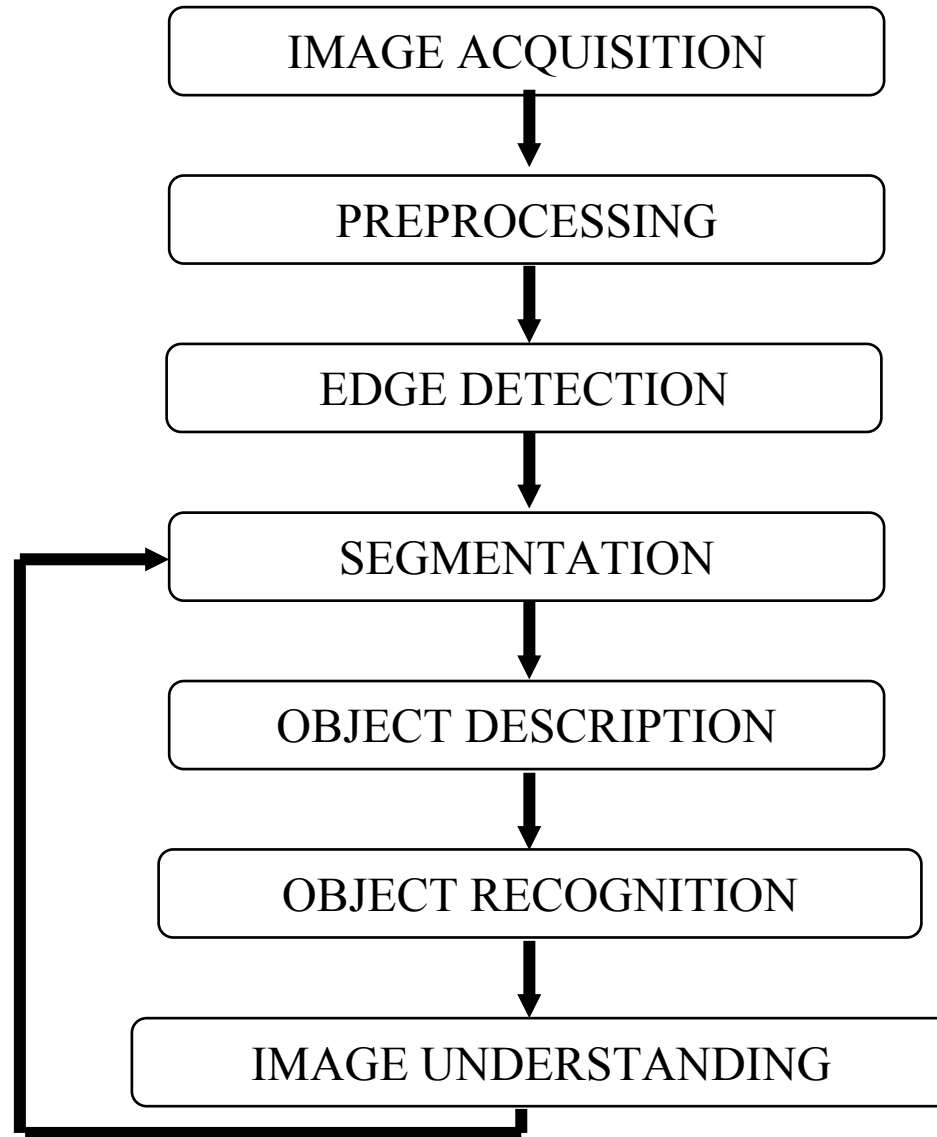
Current Subjects in Computer Science

- Definition
- Thresholding
- Frontier-based techniques

↖ Segmentation

Image segmentation refers to the decomposition of a particular scene into its fundamental components

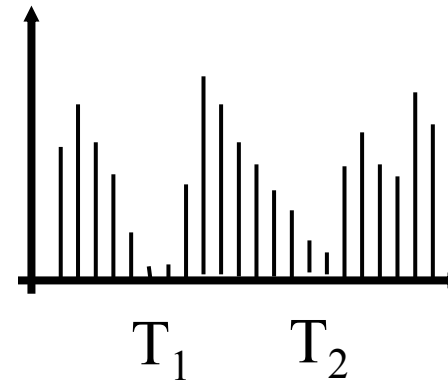
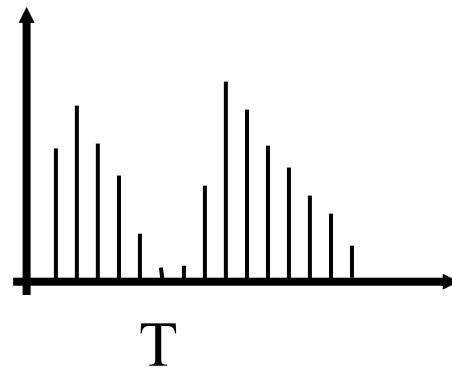
Image division in areas with some meaning



- ✓ Definition
- Thresholding
- Boundary-based techniques

↖ Fundamentals:

- ↖ Gray level is a property that may be the same for the pixels that belong to the same object.
- ↖ Each object in the scene is characterized by a particular gray value.



- ↖ We would like to select a value T that separates the image into two groups

↖ Thresholding

↖ Select a value for T that best separates the objects in the scene from the background

↖ ¿How can the threshold T be computed?

↖ Using image histogram

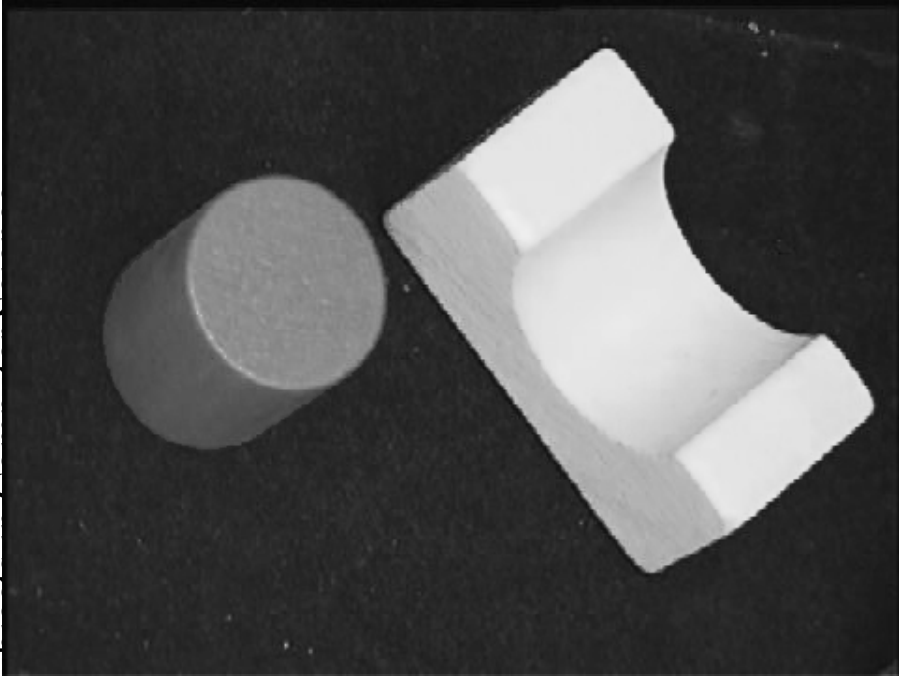
↖ Problems

☑ It may exist noise in the histogram

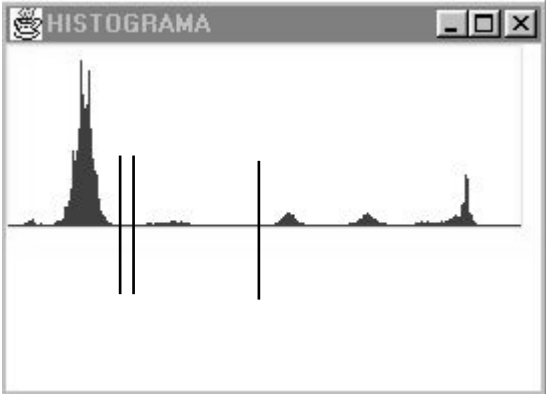
☑ There may exist little peaks and valleys in the histogram

Thresholding

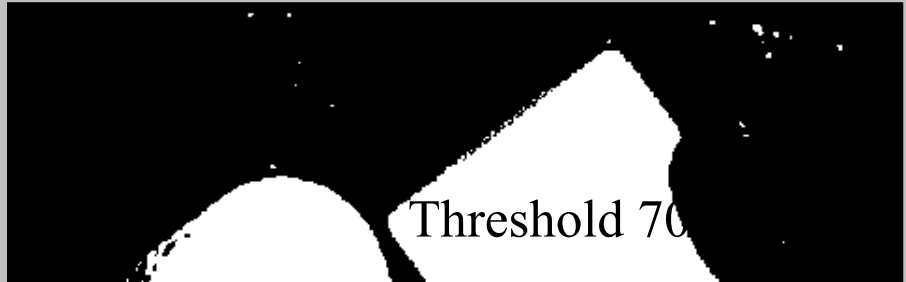
↖ Example:



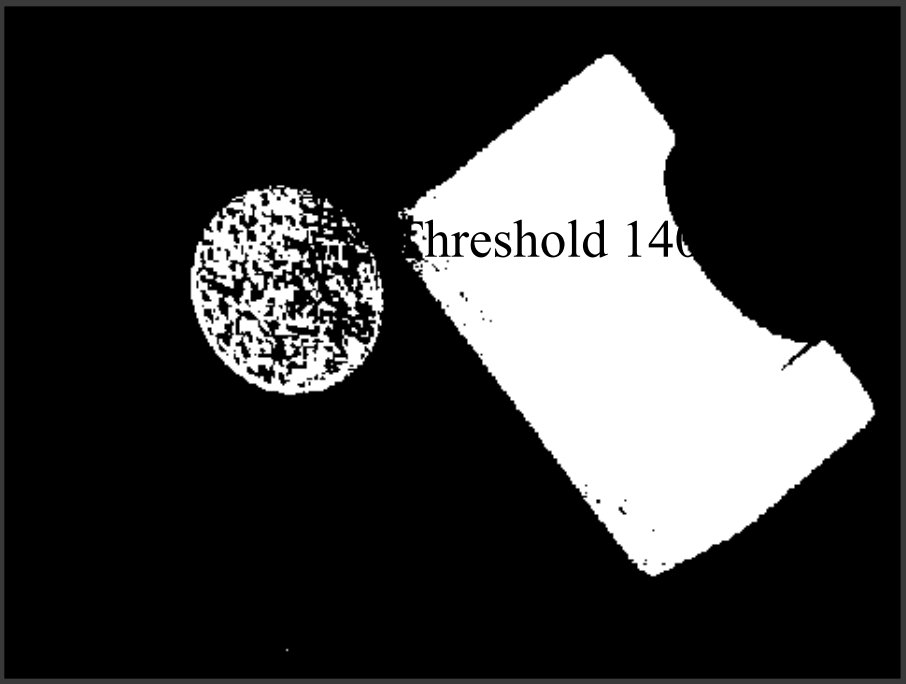
Current S



Threshold 60



Threshold 70



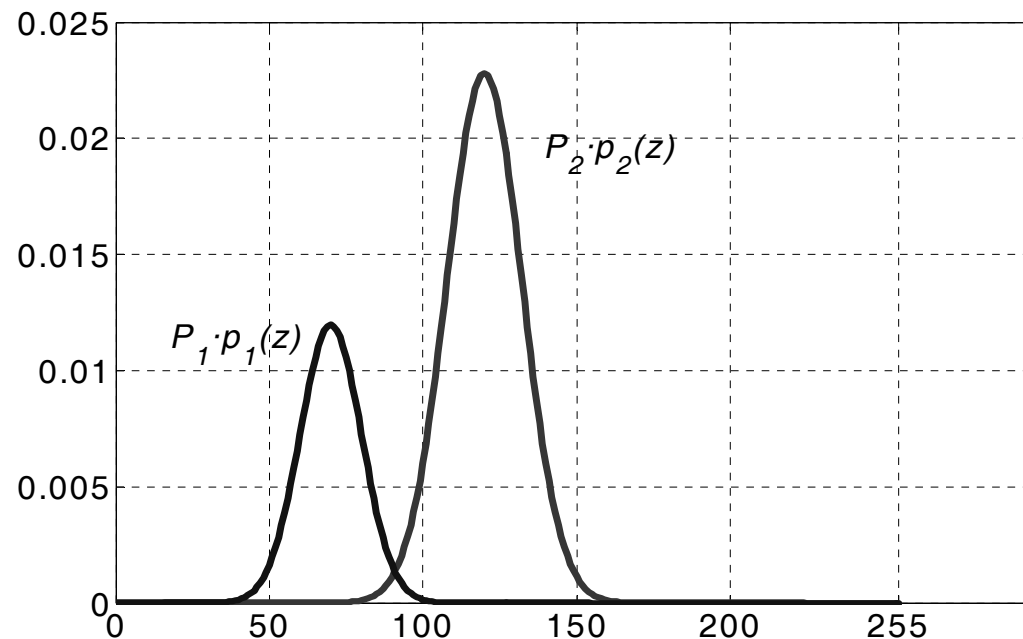
Threshold 140

↖ General outline:

↖ The histogram is formed by the probability distribution functions (pdf) of different objects in the scene.

$$p(z) = P_1 \cdot p_1(z) + P_2 \cdot p_2(z) \quad p(g) = n(g) / n_T$$

P_1 and P_2 are the *a priori* probabilities. $P_1 = n_1/n_T$ $P_2 = n_2/n_T$

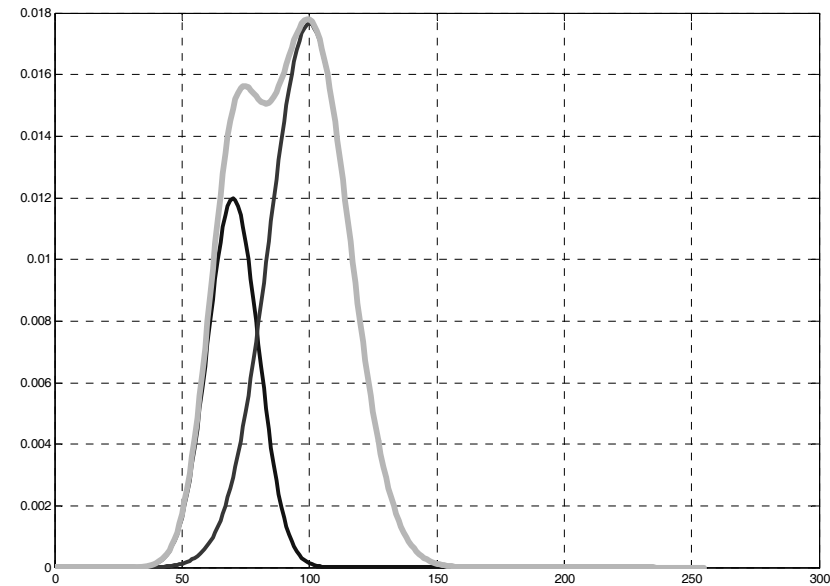
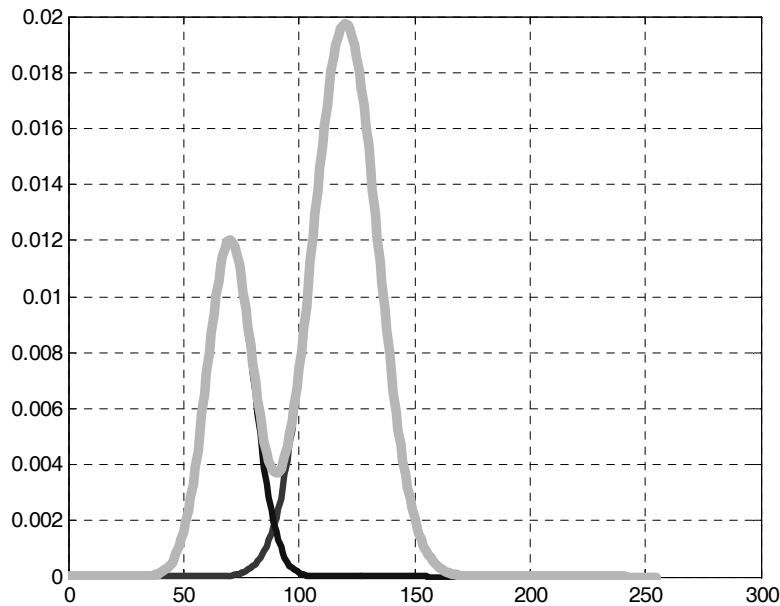


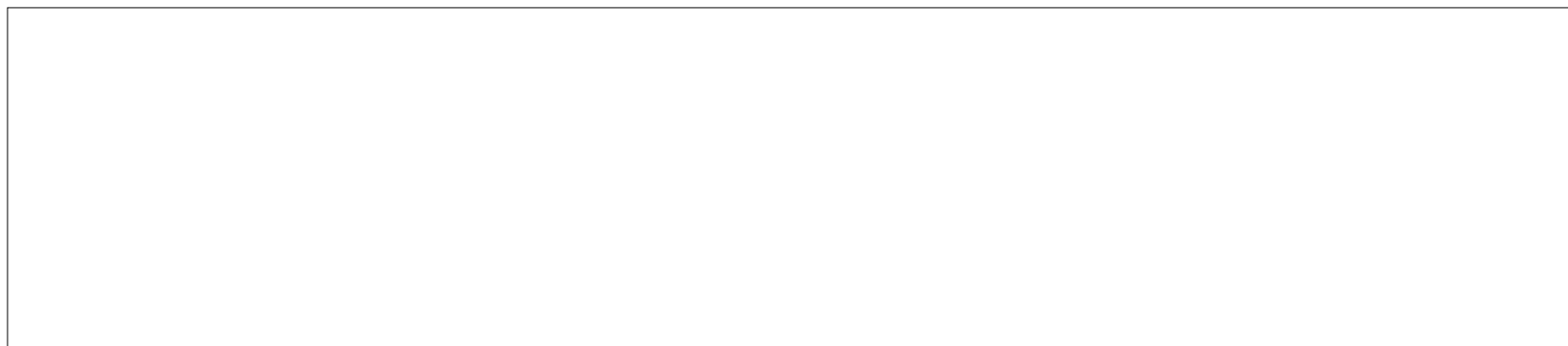
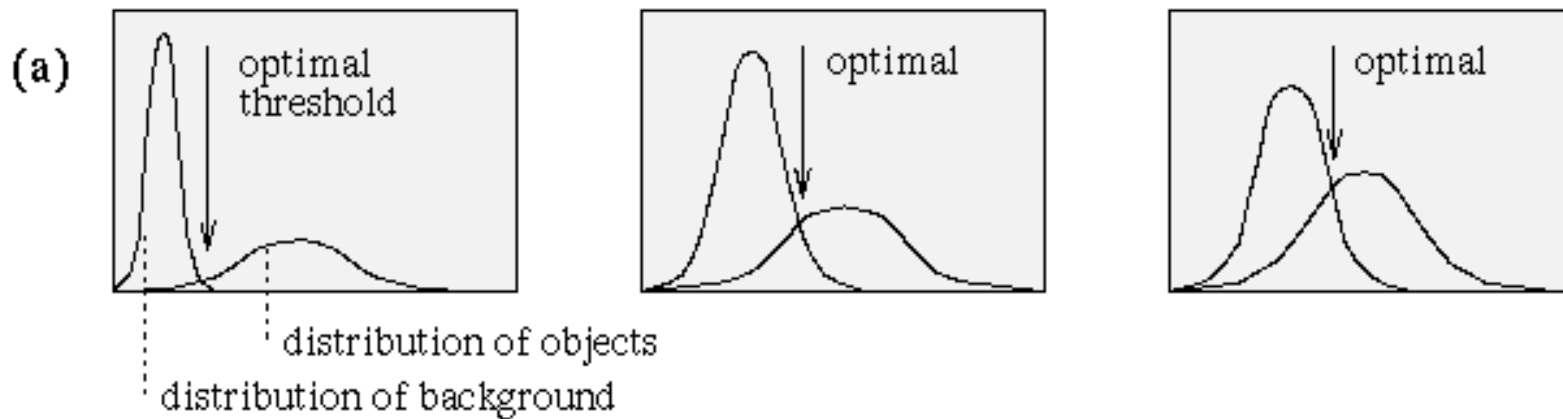
↖ The optimum value T is: $P_1 \cdot p_1(T) = P_2 \cdot p_2(T)$

↖ Problem: We don't know which pixel belongs to the object and which one belongs to the background: How can we estimate the pdf's??

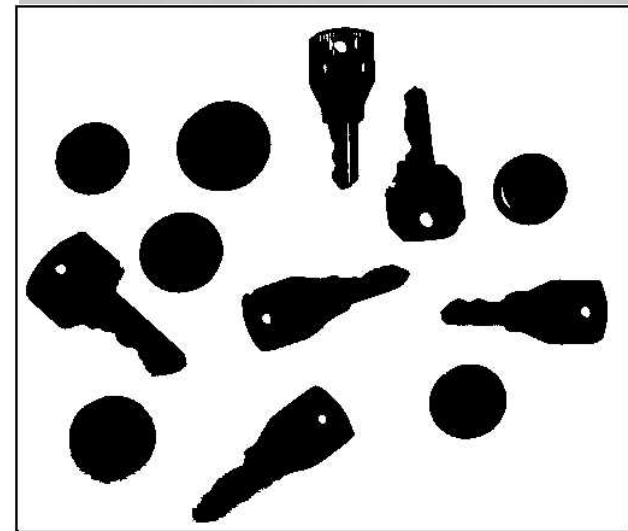
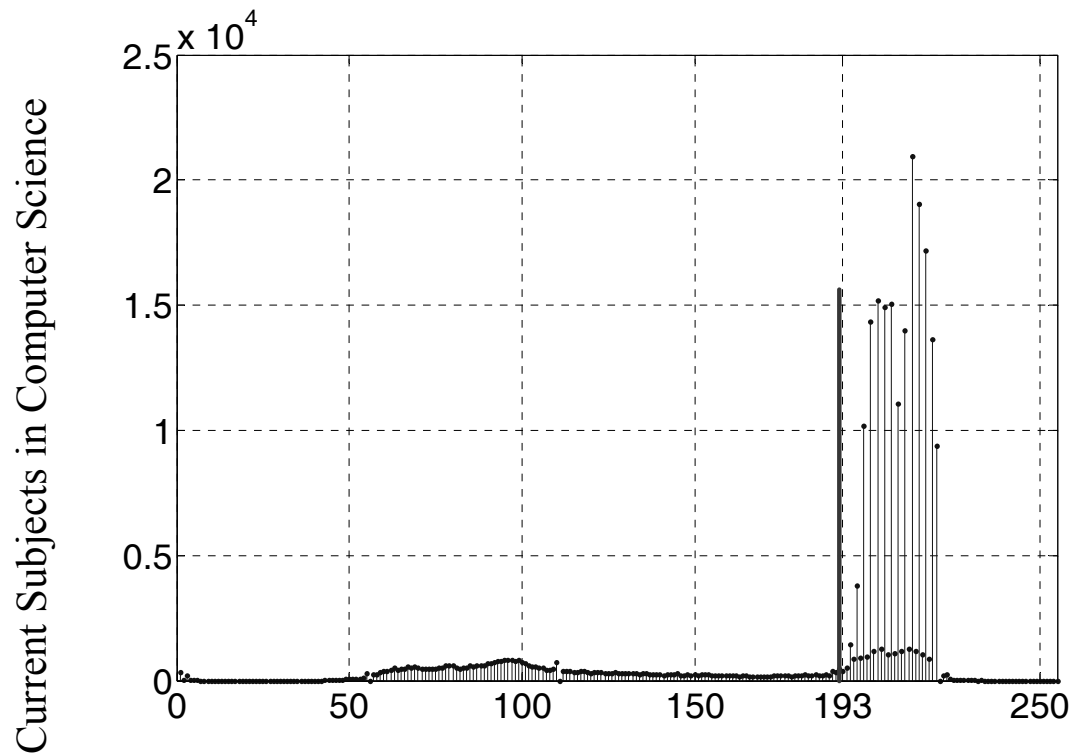
- ↖ Looking for peaks and valleys in the histogram
 - ↖ Look for maxima in the histogram
 - ↖ Look for local minima between peaks in the histogram
- ↖ Problems: ¿?
 - ↖ Noise → false minima
 - ↖ The sum of pdf's does not have a valley at the optimum value.

Current Subjects in Computer Science





↖ Global thresholding example: It is not obvious where to set T



↖ Clustering (k-means)

↖ We can look at the problem from a different point of view:

↔ Suppose we've got two different groups of pixels. Each one at a particular range.

↖ Then:

↔ A threshold T separates the image into two groups: object (o) and background (b).

↔ μ_o : Mean value of the pixels considered as object.

↔ μ_b : Mean value of the pixels considered as background.

↔ We look for a T such as:

$$\forall f(x, y) \geq T: |f(x, y) - \mu_b(T)| \geq |f(x, y) - \mu_o(T)|$$

$$\forall f(x, y) < T: |f(x, y) - \mu_b(T)| < |f(x, y) - \mu_o(T)|$$

↖ Algorithm:

- 1) Begin selecting $T^0 = B$, which separates the pixels into two groups.
- 2) Calculate the mean value in each group:

$$\mu_b^i(T^i) = \frac{\sum_{f(x,y) < T} f(x,y)}{\text{num.pixels } b} \quad \mu_o^i(T^i) = \frac{\sum_{f(x,y) \geq T} f(x,y)}{\text{num.pixels } o}$$

- 3) Select a new threshold T^i :

$$T^{i+1} = \frac{\mu_b^i + \mu_o^i}{2}$$

- 4) Goto 2).
- 5) Repeat until T stabilizes.

Current Subjects in Computer Science

- ✓ Definition
- ✓ Thresholding
- Frontier-based techniques

↖ Hough transform

- ↖ It can be regarded as a global technique
- ↖ It enables us to detect lines in an image
- ↖ Input:
 - ↖ Binary image from gradient thresholding.

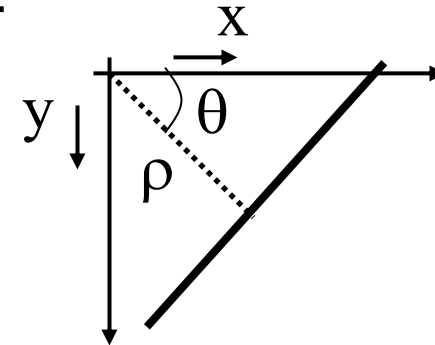
↖ Line detection

$$y = ax + b$$

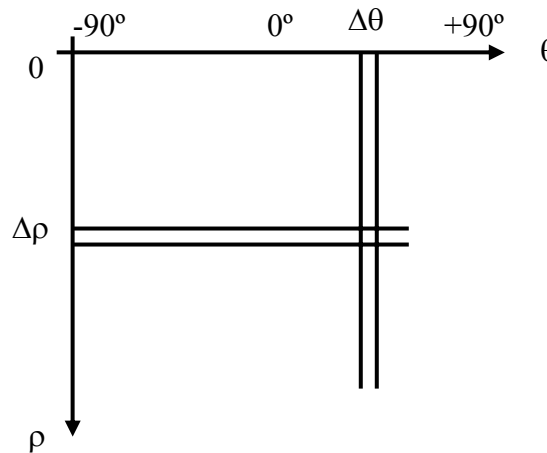
- ↖ For a line 'a' and 'b' are constant
- ↖ Given a set of points (x_i, y_i) belonging to the edge we would like to estimate the parameters 'a' and 'b'.
- ↖ What is the problem with this representation? ¿?

↖ An alternative way to represent a line:

$$\rho = x \cdot \cos(\theta) + y \cdot \sin(\theta)$$



↖ The parameters to estimate now are ρ y θ . The new space of parameters is discretized.



Algorithm:

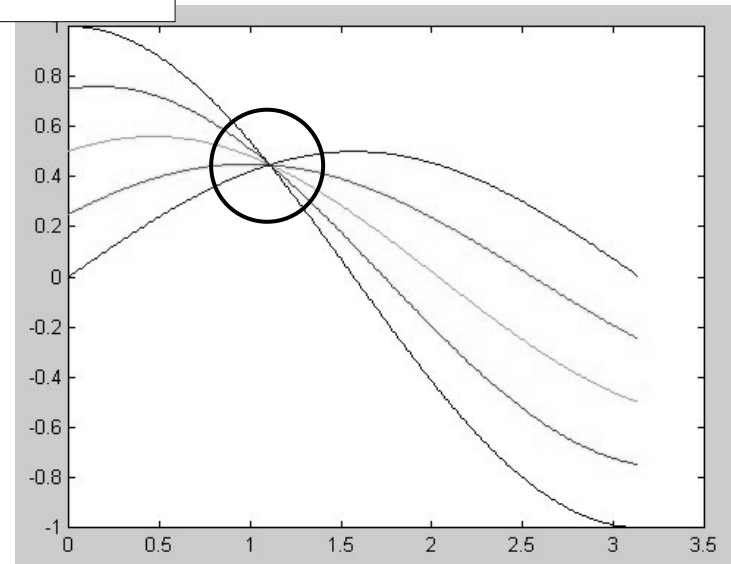
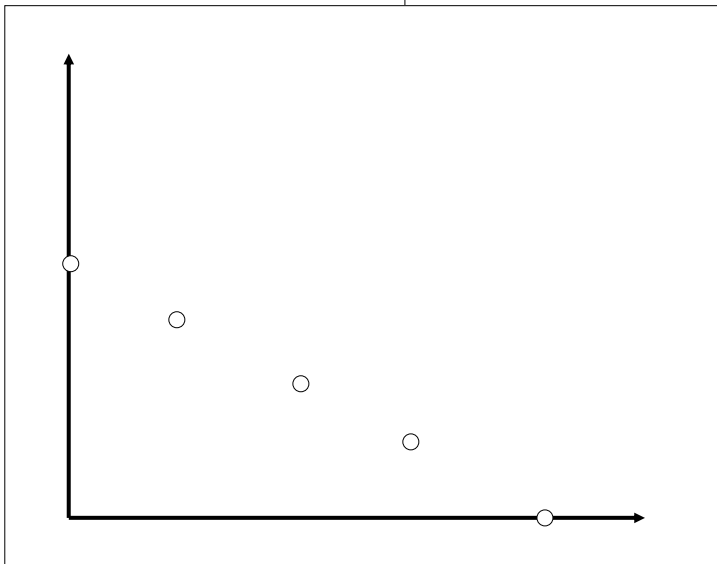
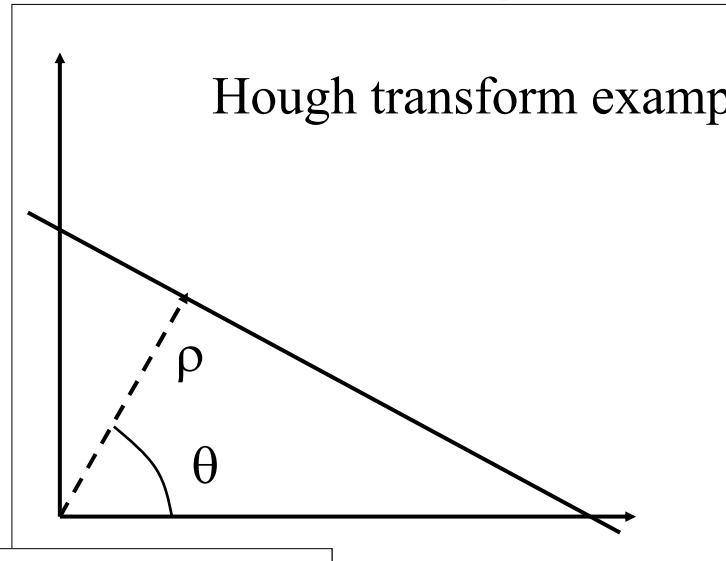
1. Define increments for ρ and θ (e.g. $\Delta\theta = 0.1$ rad)
2. For each point (x_i, y_i) belonging to the edge, compute the following equation:

$$\rho = x_i \cos \theta + y_i \sin \theta$$

¿? What next?

3. Vote for all the $\rho \theta$ that comply with the prior equation.
 - ✓ The number of votes in each cell represents the number of points (x_i, y_i) that belong to a line with parameters (ρ, θ) .
 - ✓ A threshold lets us select the lines in the image.

↖ Hough transform example



↖ Question: ¿?

⇐ How to extract n lines from the image?

